

Graph Neural Networks, Their Logic, and Formal Verification

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Outline

1 Introduction

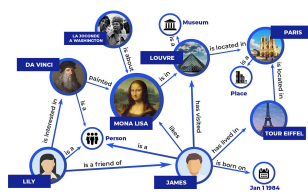
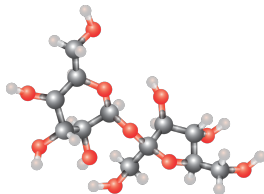
2 AC-GNNs

3 ACR-GNNs

4 Conclusions

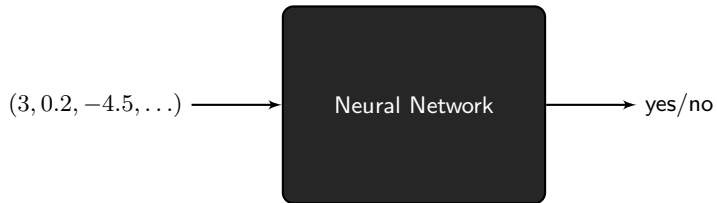
Graph Neural Networks: neural networks processing graphs. [Scarselli et al. 2009]¹

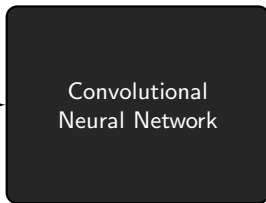
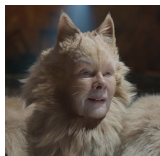
Applications in social recommendations, drug discovery, material science, financial networks anomaly detection, combinatorial optimization, etc.



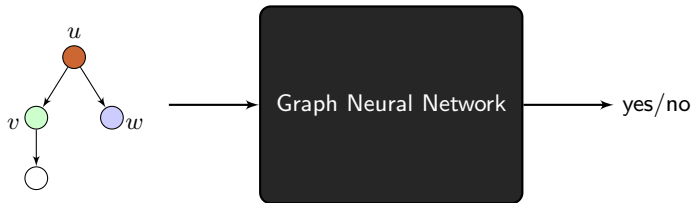
Implement a function $\tau(G, u) \in \mathbb{R}^m$, mapping a graph and one of its vertices into a m -dimensional Euclidean space; or simply a value in $\{0, 1\}$.

¹Franco Scarselli et al. "The Graph Neural Network Model". In: *IEEE Transactions on Neural Networks* 20.1 (2009), pp. 61–80.





yes/no



Research directions

- **architecture restrictions/extensions**: readout, attention, recurrent², higher-order³, ...
- **variations on numbers, aggregation, and activation functions**: real/rationals/integers/fixed bitwidth^{4,5}, bounded aggregation, eventually constant activations, ...
- **expressivity**: WL,^{6,7} relative to FO,⁸ ..., descriptive complexity,⁹ ...
- **complexity**: verification tasks
- ...

²Veeti Ahvonen, Damian Heiman, and Antti Kuusisto. "Graph neural networks and MSO". In: *CoRR* abs/2505.07816 (2025).

³Huan Luo and Jonni Virtema. "Unifying approach to uniform expressivity of graph neural networks". In: *CoRR* abs/2602.18409 (2026).

⁴Michael Benedikt et al. "Decidability of Graph Neural Networks via Logical Characterizations". In: *51st International Colloquium on Automata, Languages, and Programming, ICALP 2024*. 2024.

⁵Veeti Ahvonen et al. "Logical characterizations of recurrent graph neural networks with reals and floats". In: *NeurIPS 2024*. 2024.

⁶Martin Grohe. "The Logic of Graph Neural Networks". In: *LICS 2021*. IEEE, 2021.

⁷Pablo Barceló et al. "The Logical Expressiveness of Graph Neural Networks". In: *8th International Conference on Learning Representations (ICLR 2020)*. 2020.

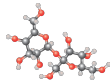
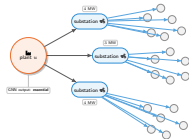
⁸Stan P. Hauke and Przemysław Andrzej Walega. "Aggregate-Combine-Readout GNNs Can Express Logical Classifiers Beyond the Logic C2". In: *AAAI 2026*. 2026.

⁹Martin Grohe. "The Descriptive Complexity of Graph Neural Networks". In: *TheoretCS* 3, 25 (2024).

GNN verification tasks

Critical domains:

- infrastructure networks
- molecules and materials
- social and financial networks
- knowledge graphs



Typical verification questions

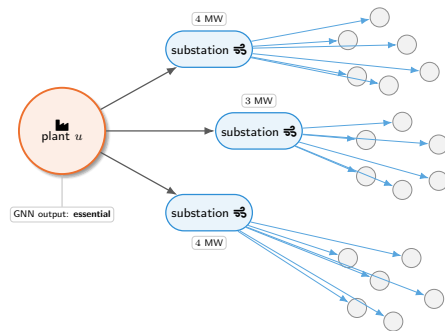
Given a (Boolean classifier) GNN $\mathcal{A}$ and a logical specification φ , decide whether:

- $[[\varphi]] \subseteq [[\mathcal{A}]]$ sufficiency
- $[[\mathcal{A}]] \subseteq [[\varphi]]$ necessity
- $[[\varphi]] \cap [[\mathcal{A}]] \neq \emptyset$ consistency

Example: essential power plants

Examples of verification: “Is it the case that...

- (sufficiency) ... any power plant serving over a 1000 users is classified by the GNN as essential?”
- (necessity) ... any power plant classified by the GNN as essential has at least 3 substations?”
- (consistency) ... a power plant classified by the GNN as essential can be a wind farm whose wind turbines have a total capacity of less than 12 MW?”



Model restrictions

We study aggregate-combine GNNs with deliberately discrete ingredients.

- finite directed labelled graphs;
- integer parameters in $\mathbb{Z}$;
- $\sum$ aggregation;
- linear combinations;
- truncated ReLU activation $\sigma(x) = \max(0, \min(1, x))$;
- linear Boolean classification.

This talk

- 1 provides some background on AC(R)-GNNs
- 2 studies the verification tasks of both AC-GNNs and ACR-GNNs.

Model	Capturing logic	Satisfiability / verification
AC-GNN	$K^\#$	PSPACE-complete
ACR-GNN	$K^{\#,\#\forall}$	NEXPTIME-complete / (co)NEXPTIME-complete

Main ideas behind the translations from GNNs to logic and back already in [Barceló et al. 2020]¹⁰.

The main contributions are in

- identifying the ‘right’ logics, and demonstrate that they have
 - ▶ right expressivity
 - ▶ right succinctness
- and establishing their complexity
 - ▶ ... identifying the right already known logics to translate them into.

¹⁰Barceló et al., “The Logical Expressiveness of Graph Neural Networks”.

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Graphs and embeddings

A (labeled directed) graph G is a tuple (V, E, ℓ) such that V is a finite set of vertices, $E \subseteq V \times V$ a set of directed edges and ℓ is a mapping from V to a valuation over a set of atomic propositions.

We write $\ell(u)(p) = 1$ when the atomic proposition p is true in u , and $\ell(u)(p) = 0$ otherwise.

Given a graph G and a vertex $u \in V$, we call (G, u) a pointed graph.

Suppose that the atomic propositions occurring in G are $p_1, \dots, p_k$. The initial embedding $\mathbf{x}_0$ is defined by:

$$\mathbf{x}_0(u) := (\ell(u)(p_1), \dots, \ell(u)(p_k)) \in \{0, 1\}^k$$

for all $u \in V$.

AC-GNN layer

At each layer, a vertex combines its current state with the sum of the states of its successors.

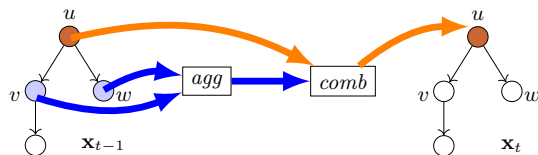
$$\mathbf{x}_t(u) := \text{comb}\left(\mathbf{x}_{t-1}(u), \text{agg}(\{\{\mathbf{x}_{t-1}(v) \mid uv \in E\}\})\right)$$

In this work:

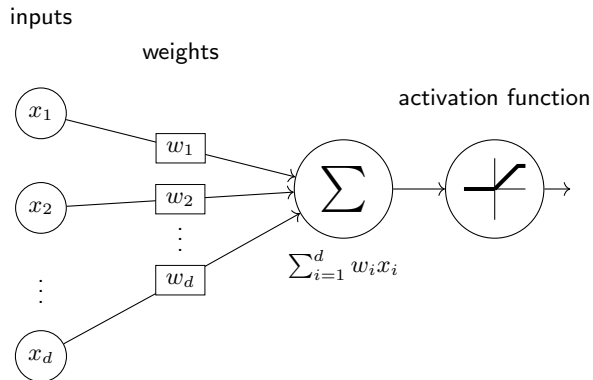
$$\text{agg}(X) = \sum_{x \in X} x$$

$$\text{comb}(x, y) = \vec{\sigma}(xC + yA + b)$$

where A and C are matrices of integer parameters, and b an integer vector.

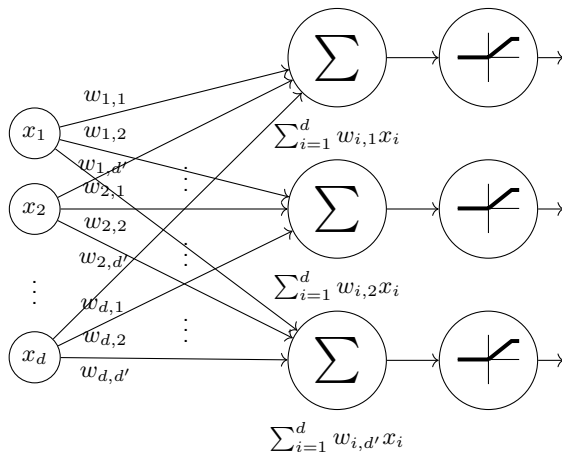


Intermission. The perceptron — a neuron with d inputs



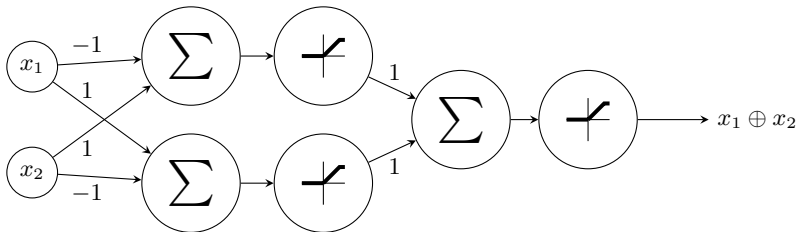
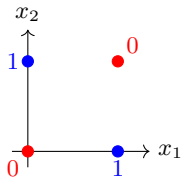
$$\vec{\sigma} \left((x_1, x_2, \dots, x_d) \begin{pmatrix} w_1 \\ w_2 \\ \vdots \\ w_d \end{pmatrix} \right)$$

Intermission. The perceptron — a layer with d inputs and d' outputs



$$\vec{\sigma} \left((x_1, x_2, \dots, x_d) \begin{pmatrix} w_{1,1} & w_{1,2} & \dots & w_{1,d'} \\ w_{2,1} & \ddots & & \\ \vdots & & & \\ w_{d,1} & w_{d,2} & \dots & w_{d,d'} \end{pmatrix} \right)$$

Intermission. XOR with a multilayer perceptron

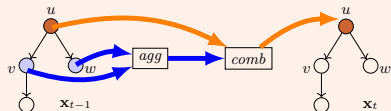


Example

Consider a layer $\mathcal{L}^{(t)}$ with input dimension 2 and output dimension 3, defined by:

■ $agg(X) := \sum_{\mathbf{x} \in X} \mathbf{x}$,

■ $C = \begin{pmatrix} -1 & -2 & 0 \\ 3 & 0 & -4 \end{pmatrix}$, $A = \begin{pmatrix} 5 & 0 & 0 \\ -6 & 7 & 0 \end{pmatrix}$, and $b = (8 \ 9 \ 10)$



Suppose that vertex u has two successors v and w .

■ $\mathbf{x}_{t-1}(u) = (1, 3)$, $\mathbf{x}_{t-1}(v) = (1, 1)$, $\mathbf{x}_{t-1}(w) = (0, 1)$

First, $\mathbf{y} = agg(\{\{\mathbf{x}_{t-1}(v), \mathbf{x}_{t-1}(w)\}\}) = \mathbf{x}_{t-1}(v) + \mathbf{x}_{t-1}(w) = (1, 1) + (0, 1) = (1, 2)$.

Second,

$$\mathbf{x}_t(u) = comb(\mathbf{x}_{t-1}(u), \mathbf{y}) = \vec{\sigma}(\mathbf{x}_{t-1}(u)C + \mathbf{y}A + b)$$

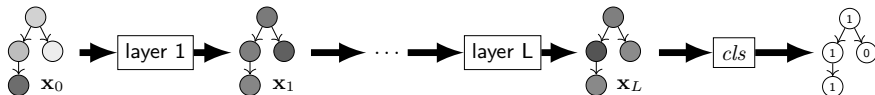
$$\mathbf{x}_t(u) = \vec{\sigma}((1, 3) \cdot C + (1, 2) \cdot A + b) = (\sigma(9), \sigma(21), \sigma(-2)) = (1, 1, 0)$$

Semantics of a GNN

Let $\mathcal{A} = (\mathcal{L}^{(1)}, \dots, \mathcal{L}^{(L)}, cls)$.

The semantics $[[\mathcal{A}]]$ is the set of pointed graphs (G, u) such that the classifier accepts the final state of u :

$$(G, u) \in [[\mathcal{A}]] \quad \text{iff} \quad cls(\mathbf{x}_L(u)) = 1.$$



Intermission. Relationship with the Weisfeiler-Leman test

Weisfeiler-Leman (WL) test: heuristic for the graph isomorphism problem [Weisfeiler, Leman 1968]

- color every vertex u of the graph with the same color $c(u) = 1$
- iteratively assign a new color $c(u) = (c(u), \{\{c(v) \mid uv \in E\}\})$, until the color partition stabilizes

If the WL test assigns different sets of colors to two graphs, they are not isomorphic.

Similar to AC-GNNs with injective aggregation and combination functions [Xu et al. 2019]¹¹, [Morris et al. 2023]¹²

If WL test assigns the same color to two nodes of a graph, then every AC-GNN classifies them identically.

¹¹Keyulu Xu et al. "How Powerful are Graph Neural Networks?" In: *ICLR 2019*. 2019.

¹²Christopher Morris et al. "Weisfeiler and Leman go Machine Learning: The Story so far". In: *Journal of Machine Learning Research* 24.333 (2023).

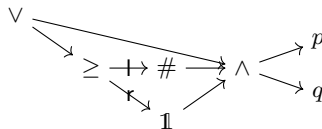
The logic $K^\#$

The logic adds integer linear constraints over two kinds of quantities.

$$\begin{aligned}\varphi &::= p \mid \neg\varphi \mid \varphi \vee \varphi \mid \xi \geq 1 \\ \xi &::= c \mid \mathbb{1}\varphi \mid \#\varphi \mid \xi + \xi \mid c \times \xi\end{aligned}$$

Formulas as DAGs: E.g.,

$$(p \wedge q) \vee (\#(p \wedge q) \geq \mathbb{1}(p \wedge q))$$



Semantics:

- $[[\mathbb{1}\varphi]]_{G,u}$ is 1 if φ holds at vertex u , and 0 otherwise.
- $[[\#\varphi]]_{G,u}$ counts successors of u satisfying φ .

Simulating (graded) modal logic

$$\Box\varphi := (-1) \times \#(\neg\varphi) + 1 \geq 1$$

$$\Diamond^{\geq k}\varphi := \#\varphi + (-1) \times k + 1 \geq 1$$

Some expressivity beyond FOL

“There are at least as many p -successors as q -successors” is $\#p \geq \#q$, or:

$$\#p + (-1) \times \#q + 1 \geq 1$$

Equivalence: AC-GNNs and $K^\#$

Theorem

For every $K^\#$ -formula φ , one can compute in polynomial time a GNN $\mathcal{A}_\varphi$ such that $[[\varphi]] = [[\mathcal{A}_\varphi]]$.

Theorem

For every AC-GNN $\mathcal{A}$, one can compute in polynomial time a $K^\#$ -formula $\varphi_{\mathcal{A}}$ such that $[[\mathcal{A}]] = [[\varphi_{\mathcal{A}}]]$.

$K^\# \iff$ AC-GNN Boolean classifiers

Translation idea: logic $\rightarrow$ GNN

Enumerate subformulas of φ : $\varphi_1 = p_1, \dots, \varphi_m = p_m, \dots, \varphi_n = \varphi$.

Build n identical layers, with $n \times n$ matrices A and C , such that:

- $C_{ii} = 1$ if $i \leq m$,
- $C_{ji} = -1, b_i = 1$ if $\varphi_i = \neg\varphi_j$,
- $C_{ji} = C_{li} = 1$ if $\varphi_i = \varphi_j \vee \varphi_l$, and
- $C_{ji} = k_j, A_{j'i} = k'_{j'}, b_i = c$
 for all $j \in J, j' \in J'$ if $\varphi_i = \sum_{j \in J} k_j \times \mathbb{1}\varphi_j + \sum_{j' \in J'} k'_{j'} \times \#\varphi_{j'} + c \geq 1$.
- $C_{ji} = A_{ji} = 0$ otherwise

We use the classification function $cls(x) = x_n \geq 1$.

From logic to GNN (example)

Example

Consider the formula $\varphi = \neg(p \vee (8 \leq 3 \times \#q))$. We define the following GNN $\mathcal{A}$ which is equivalent to φ as follows. We first consider the following subformulas of φ in that order:

φ_1	φ_2	φ_3	φ_4	φ_5
p	q	$8 \leq 3 \times \#q \equiv 3 \times \#q + (-7) \geq 1$	$\varphi_1 \vee \varphi_3$	$\neg \varphi_4$

The combination function for all layers is $comb(x, y) = \vec{\sigma}(xC + yA + b)$ where

$$C = \begin{pmatrix} 1 & 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & -1 \\ 0 & 0 & 0 & 0 & 0 \end{pmatrix}, A = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 3 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \end{pmatrix}, \text{ and } b = (0 \quad 0 \quad -7 \quad 0 \quad 1).$$

Translation idea: GNN $\rightarrow$ logic

For each layer t and output coordinate j , build a formula $\varphi_{t,j}$ that says:

“output coordinate j of vertex u after layer t is 1”.

The formula mirrors the layer equation:

$$\varphi_{t,j} = \sum_{k=1}^{d_t} C_{kj} \times \mathbb{1}\varphi_{t-1,k} + \sum_{k=1}^{d_t} A_{kj} \times \#\varphi_{t-1,k} + b_j \geq 1.$$

In the end, we set $\varphi_{\mathcal{A}} = a_1 \times \mathbb{1}\varphi_{L,1} + \dots + a_{d'_L} \times \mathbb{1}\varphi_{L,d'_L} \geq 1$.

From GNN to logic (example)

Example

- Suppose we have two propositions p_1, p_2 : the two formulas that represent state $\mathbf{x}_0$ are $\varphi_{01} = p_1$ and $\varphi_{02} = p_2$.

- Suppose we have two layers, given by the same combination and aggregation functions:

$$\mathbf{x}_1(u) = \text{comb}(\mathbf{x}_0(u), \text{agg}(\{\{\mathbf{x}_0(v) | uv \in E\}\})) \quad \mathbf{x}_2(u) = \text{comb}(\mathbf{x}_1(u), \text{agg}(\{\{\mathbf{x}_1(v) | uv \in E\}\}))$$

with aggregation function $\text{agg}(X) = \sum_{x \in X} x$, and combination function

$$\text{comb}((x, x'), (y, y')) = \vec{\sigma} \left((x \quad x') \begin{pmatrix} 1 & 6 \\ 2 & 7 \end{pmatrix} + (y \quad y') \begin{pmatrix} -3 & 8 \\ 4 & 9 \end{pmatrix} + (5 \quad 10) \right)$$

The formulas that represent the state $\mathbf{x}_1$ are formula

$$\varphi_{11} = 1 \times \mathbb{1}\varphi_{01} + 2 \times \mathbb{1}\varphi_{02} - 3\#\varphi_{01} + 4\#\varphi_{02} + 5 \geq 1 \text{ and formula}$$

$$\varphi_{12} = 6 \times \mathbb{1}\varphi_{01} + 7 \times \mathbb{1}\varphi_{02} + 8\#\varphi_{01} - 9\#\varphi_{02} + 10 \geq 1.$$

The formulas that represent the state $\mathbf{x}_2$ are formula

$$\varphi_{21} = 1 \times \mathbb{1}\varphi_{11} + 2 \times \mathbb{1}\varphi_{12} - 3\#\varphi_{11} + 4\#\varphi_{12} + 5 \geq 1 \text{ and formula}$$

$$\varphi_{22} = 6 \times \mathbb{1}\varphi_{11} + 7 \times \mathbb{1}\varphi_{12} + 8\#\varphi_{11} - 9\#\varphi_{12} + 10 \geq 1.$$

- Suppose that the classification function is given by $\text{cls}(x, x') = 5x - 3x' \geq 1$.

The formula $\varphi_{\mathcal{A}}$ that represents the GNN $\mathcal{A}$ is $5 \times \mathbb{1}\varphi_{21} - 3 \times \mathbb{1}\varphi_{22} \geq 1$.

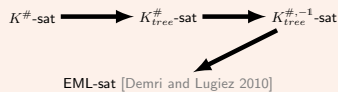
Complexity of $K^\#$ satisfiability

Theorem

The satisfiability problem of $K^\#$ is PSPACE-complete.

Upper bound intuition

Reduce $K^\#$ satisfiability to Extended Modal Logic satisfiability [Demri and Lugiez 2010]^a.



^aStéphane Demri and Denis Lugiez. "Complexity of modal logics with Presburger constraints". In: *J. Appl. Log.* (2010).

Lower bound intuition

Modal logic K embeds into $K^\#$, and K -satisfiability is PSPACE-hard.

Complexity of AC-GNN verification

Corollary

The problems sufficiency, necessity and consistency are in PSPACE.

Proof.

E.g., for necessity: given $\mathcal{A}$, φ , we can check that $[[\mathcal{A}]] \subseteq [[\varphi]]$, by computing the $K^\#$ -formula $\varphi_{\mathcal{A}} \rightarrow \varphi$ and then check that $\varphi_{\mathcal{A}} \rightarrow \varphi$ is valid. □

Theorem

The problems sufficiency, necessity and consistency are PSPACE-complete.

Proof.

Poly-time reductions from the satisfiability/unsatisfiability/validity of a $K^\#$ -formula. Consider $\mathcal{A}_{all}$ a GNN that accepts all graphs, and $\mathcal{A}_{none}$ a GNN that rejects all graphs.

- sufficiency: $[[\varphi]] \subseteq [[\mathcal{A}_{none}]]$ iff φ is unsatisfiable
- necessity: $[[\mathcal{A}_{all}]] \subseteq [[\varphi]]$ iff φ is valid
- consistency: $[[\varphi]] \cap [[\mathcal{A}_{all}]] \neq \emptyset$ iff φ is satisfiable

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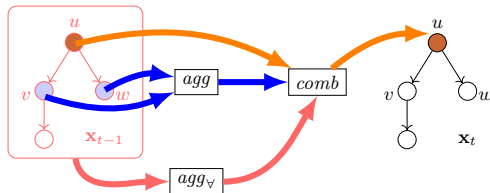
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Adding readout: ACR-GNNs

An ACR-GNN layer adds a global aggregation/readout term.



$$\mathbf{x}_t(u) := \text{comb}\left(\mathbf{x}_{t-1}(u), \text{agg}(\{\{\mathbf{x}_{t-1}(v) \mid uv \in E\}\}), \text{agg}_{\forall}(\{\{\mathbf{x}_{t-1}(v) \mid v \in V\}\})\right)$$

$$\text{agg}_{\forall}(X) = \sum_{x \in X} x$$

$$\text{comb}(x, y, z) = \vec{\sigma}(xC + yA + zR + b)$$

The logic $K^{\#, \# \forall}$

Extend $K^{\#}$ with global counting:

$$\begin{aligned}\varphi &::= p \mid \neg \varphi \mid \varphi \vee \varphi \mid \xi \geq 1 \\ \xi &::= c \mid \mathbb{1}\varphi \mid \#\varphi \mid \# \forall \varphi \mid \xi + \xi \mid c \times \xi.\end{aligned}$$

$$[[\# \forall \varphi]]_{G,u} = |\{v \in V \mid (G, v) \models \varphi\}|.$$

Example

“a windfarm who serves at least half of all users”:

$$\text{windfarm} \wedge (2 \times \#\text{user} - \# \forall \text{user} + 1 \geq 1)$$

Equivalence: ACR-GNNs and $K^{\#,\#_{\forall}}$

Theorem

For every ACR-GNN $\mathcal{A}$, one can compute in polynomial time a $K^{\#,\#_{\forall}}$ -formula $\varphi_{\mathcal{A}}$ such that $[[\mathcal{A}]] = [[\varphi_{\mathcal{A}}]]$.

Theorem

For every $K^{\#,\#_{\forall}}$ -formula φ , one can compute in polynomial time an ACR-GNN $\mathcal{A}_{\varphi}$ such that $[[\varphi]] = [[\mathcal{A}_{\varphi}]]$.

$K^{\#,\#_{\forall}} \iff$ ACR-GNN Boolean classifiers

Complexity of ACR-GNNs verification

Theorem

The satisfiability problem of $K^{\#,\#_{\forall}}$ is NEXPTIME-complete.

Upper bound intuition

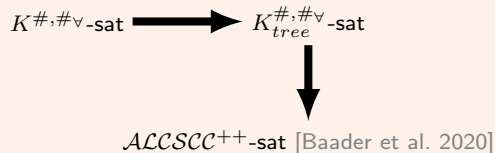
Reduce $K^{\#,\#_{\forall}}$ satisfiability to $\mathcal{ALCSCC}^{++}$ satisfiability [Baader, Bednarczyk, Rudolph 2020].

A QFBAPA formula is a Boolean combination of:

- **set constraints**: e.g., $Windfarm \subseteq Powerplant$
- **cardinality constraints**: e.g.,
 $|Windfarm \cup SolarPlant| \leq |ThermalPlant|$

$\mathcal{ALCSCC}^{++}$ extends $\mathcal{ALC}$ with concepts such as::

- $Windfarm \sqcap \text{sat}(|User| \leq 2 \times |serves \sqcap User|)$



Lower bound intuition

Reduce from $\mathcal{ALCQ}\text{-}T_C\text{Box}$ consistency [Tobies 2000]^a.

^aStephan Tobies. "The Complexity of Reasoning with Cardinality Restrictions and Nominals in Expressive Description Logics". In: *J. Artif. Intell. Res.* 12 (2000).

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Verification of GNNs

There is hope for the formal verification of GNNs.

The logical equivalences turn GNN verification into satisfiability checking.

Question	Logical test	AC-GNN	ACR-GNN
Sufficiency	$\varphi \rightarrow \varphi_{\mathcal{A}}$ valid	PSPACE	coNEXPTIME
Necessity	$\varphi_{\mathcal{A}} \rightarrow \varphi$ valid	PSPACE	coNEXPTIME
Consistency	$\varphi \wedge \varphi_{\mathcal{A}}$ satisfiable	PSPACE	NEXPTIME

AC(R)-GNNs with quantized types

Real neural-network implementations use finite computer number formats rather than mathematical integers.

Proposition

The reasoning problems for AC-GNNs over finite computer number formats such as FP32 or INT8 remain PSPACE-complete.

Proposition

The reasoning problems for ACR-GNNs over finite computer number formats such as FP32 or INT8 remain (co)NEXPTIME-complete.

Related work

- Extended Modal Logic: [Demri and Lugiez 2010]¹³
- Description logics with cardinality and set constraints: [Baader, Bednarczyk, Rudolph 2020]¹⁴
- QFBAPA: [Kuncak and Rinard 2007]¹⁵
- Similar and more general GNN/logical characterizations: [Benedikt, Lu, Motik, and Tan 2024]¹⁶; [Benedikt, Lu, and Tan 2026]¹⁷
- $K^\#$ -like logic for transformers: [Yang and Chiang 2024]¹⁸

¹³Demri and Lugiez, “Complexity of modal logics with Presburger constraints”.

¹⁴Franz Baader, Bartosz Bednarczyk, and Sebastian Rudolph. “Satisfiability and Query Answering in Description Logics with Global and Local Cardinality Constraints”. In: *ECAI 2020*. 2020.

¹⁵Viktor Kuncak and Martin Rinard. “Towards Efficient Satisfiability Checking for Boolean Algebra with Presburger Arithmetic”. In: *CADE-21*. 2007.

¹⁶Benedikt et al., “Decidability of Graph Neural Networks via Logical Characterizations”.

¹⁷Michael Benedikt, Chia-Hsuan Lu, and Tony Tan. “Decidability of Graph Neural Networks via Logical Characterizations”. In: *ACM Trans. Comput. Logic* (2026).

¹⁸Andy Yang and David Chiang. “Counting Like Transformers: Compiling Temporal Counting Logic Into Softmax Transformers”. In: *COLM*. 2024.

Papers

■ AC-GNNs:

- ▶ Pierre Nunn et al. “A Logic for Reasoning about Aggregate-Combine Graph Neural Networks”. In: *IJCAI 2024*. 2024
- ▶ Marco Sälzer, François Schwarzentruher, and Nicolas Troquard. “Verifying Quantized Graph Neural Networks is PSPACE-complete”. In: *IJCAI 2025*. 2025

■ ACR-GNNs: Artem Chernobrovkin et al. “Verifying Quantized GNNs With Readout Is Decidable But Highly Intractable”. In: *KR 2026*. 2026

GNNs and logic at FLoC

- invited talk at KR ([Carsten Lutz](#) – *The Logical Expressive Power of Graph Neural Networks*)
- invited talk at OVERLAY ([Przemysław Wałęga](#) – *Preservation Theorems: From Tarski to Graph Neural Networks*)
- invited talk at LOGICNN ([Martin Grohe](#) – *Logic and the Power of Recurrent Graph Neural Networks*)
- Several papers at KR
- Several papers at LOGICNN

Workshop on Logical Methods for Neural Network Analysis
Lisbon, July 25, 2026

FEDERATED LOGIC CONFERENCE

INVITED SPEAKER

Martin Grohe
RWTH Aachen University
Germany
Logic and the Power of Recurrent Graph Neural Networks

INVITED TUTORIAL SPEAKER

Omri Isac
Hebrew University of Jerusalem
Israel
Verification of DNNs with Marabou

Graph Neural Networks, Their Logic, and Formal Verification

Nicolas Troquard ¹

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joint work with Artem Chernobrovkin, Marco Sälzer, François Schwarzentruher